



# Sky Tutorials

fly beyond the sky...


**IIT-JEE | NEET | Foundation**

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## CLASSROOM CONTACT PROGRAMME

(ACADEMIC SESSION 2023-2024)

**XI – JEE**

Test Type: Chapter wise Test

Date: 05/10/2023

**MATHEMATICS**

*Duration of test 75 min and questions Paper contains 30 questions. The maximum marks are 100.*

*This Question paper contain Physics which is further divided into two sections.*

*Section –A contains 20 Questions Section B contains 10 questions. Please ensure that the Questions paper you have received contains ALL THE QUESTIONS in each Part.*

*In Section A all the 20 Questions are compulsory and in Section B Contain 10 Question, out of these 10 Questions, candidates can choose to attempt any 5 Questions.*

*Each Question has four choices (a), (b), (c), (d) out of which only one is correct & Carry 4 marks each 1 mark will be deducted for each wrong answer.*

*If you want to attempt any question then circle should be properly darkened as shown below, otherwise leave blank.*



Name of Candidate ..... ID. No .....

Candidate's Signature: ..... Invigilator's Signature: .....

**DO MORE AND MORE PRACTICE, BECAUSE PRACTICE IS THE ONLY WAY TO ACCURACY.**

**MATHEMATICS**
**SECTION - A**

- If  $\sec \theta + \tan \theta = p$ , then  $\tan \theta$  is equal to
  - $\frac{2p}{p^2 - 1}$
  - $\frac{p^2 - 1}{2p}$
  - $\frac{p^2 + 1}{2p}$
  - $\frac{2p}{p^2 + 1}$
- Which of the following is correct
  - $\tan 1 > \tan 2$
  - $\tan 1 = \tan 2$
  - $\tan 1 < \tan 2$
  - $\tan 1 = 1$
- $(m+2)\sin \theta + (2m-1)\cos \theta = 2m+1$ , if
  - $\tan \theta = \frac{3}{4}$
  - $\tan \theta = \frac{4}{3}$
  - $\tan \theta = \frac{2m}{m^2 + 1}$
  - None of these
- If  $\sin A, \cos A$  and  $\tan A$  are in G.P., then  $\cos^3 A + \cos^2 A$  is equal to
  - 1
  - 2
  - 4
  - None of these
- If  $\theta$  lies in the second quadrant, then the value of  $\sqrt{\frac{1 - \sin \theta}{1 + \sin \theta}} + \sqrt{\frac{1 + \sin \theta}{1 - \sin \theta}}$ 
  - $2 \sec \theta$
  - $-2 \sec \theta$
  - $2 \operatorname{cosec} \theta$
  - None of these
- The value of  $6(\sin^6 \theta + \cos^6 \theta) - 9(\sin^4 \theta + \cos^4 \theta) + 4$  is
  - 3
  - 0
  - 1
  - 3
- The sum  $S = \sin \theta + \sin 2\theta + \dots + \sin n\theta$ , equals
  - $\sin \frac{1}{2}(n+1)\theta \sin \frac{1}{2}n\theta / \sin \frac{\theta}{2}$
  - $\cos \frac{1}{2}(n+1)\theta \sin \frac{1}{2}n\theta / \sin \frac{\theta}{2}$
  - $\sin \frac{1}{2}(n+1)\theta \cos \frac{1}{2}n\theta / \sin \frac{\theta}{2}$
  - $\cos \frac{1}{2}(n+1)\theta \cos \frac{1}{2}n\theta / \sin \frac{\theta}{2}$
- If  $x = \cos 10^\circ \cos 20^\circ \cos 40^\circ$ , then the value of  $x$  is
  - $\frac{1}{4} \tan 10^\circ$
  - $\frac{1}{8} \cot 10^\circ$
  - $\frac{1}{8} \operatorname{cosec} 10^\circ$
  - $\frac{1}{8} \sec 10^\circ$
- Minimum value of  $5 \sin^2 \theta + 4 \cos^2 \theta$  is
  - 1
  - 2
  - 3
  - 4
- If  $\frac{3\pi}{4} < \alpha < \pi$ , then  $\sqrt{\operatorname{cosec}^2 \alpha + 2 \cot \alpha}$  is equal to
  - $1 + \cot \alpha$
  - $1 - \cot \alpha$
  - $-1 - \cot \alpha$
  - $-1 + \cot \alpha$
- $1 + \cos 56^\circ + \cos 58^\circ - \cos 66^\circ =$ 
  - $2 \cos 28^\circ \cos 29^\circ \cos 33^\circ$
  - $4 \cos 28^\circ \cos 29^\circ \cos 33^\circ$
  - $4 \cos 28^\circ \cos 29^\circ \sin 33^\circ$
  - $2 \cos 28^\circ \cos 29^\circ \sin 33^\circ$
- If  $\sin^2 \theta - 2 \cos \theta + \frac{1}{4} = 0$ , then the general value of  $\theta$  is
  - $n\pi \pm \frac{\pi}{3}$
  - $2n\pi \pm \frac{\pi}{3}$
  - $2n\pi \pm \frac{\pi}{6}$
  - $n\pi \pm \frac{\pi}{6}$
- If  $\cos 7\theta = \cos \theta - \sin 4\theta$ , then the general value of  $\theta$  is
  - $\frac{n\pi}{4}, \frac{n\pi}{3} + \frac{\pi}{18}$
  - $\frac{n\pi}{3}, \frac{n\pi}{3} + (-1)^n \frac{\pi}{18}$
  - $\frac{n\pi}{4}, \frac{n\pi}{3} + (-1)^n \frac{\pi}{18}$
  - $\frac{n\pi}{6}, \frac{n\pi}{3} + (-1)^n \frac{\pi}{18}$
- The general value of  $\theta$  satisfying the equation  $2 \sin^2 \theta - 3 \sin \theta - 2 = 0$  is
  - $n\pi + (-1)^n \frac{\pi}{6}$
  - $n\pi + (-1)^n \frac{\pi}{2}$
  - $n\pi + (-1)^n \frac{5\pi}{6}$
  - $n\pi + (-1)^n \frac{7\pi}{6}$
- General solution of  $\tan 5\theta = \cot 2\theta$  is
  - $\theta = \frac{n\pi}{7} + \frac{\pi}{14}$
  - $\theta = \frac{n\pi}{7} + \frac{\pi}{5}$
  - $\theta = \frac{n\pi}{7} + \frac{\pi}{2}$
  - $\theta = \frac{n\pi}{7} + \frac{\pi}{3}, n \in \mathbb{Z}$
- If  $\tan \theta + \tan 2\theta + \sqrt{3} \tan \theta \tan 2\theta = \sqrt{3}$ , then
  - $\theta = (6n+1)\pi / 18, \forall n \in \mathbb{I}$
  - $\theta = (6n+1)\pi / 9, \forall n \in \mathbb{I}$
  - $\theta = (3n+1)\pi / 9, \forall n \in \mathbb{I}$
  - None of these

17. If  $\frac{\tan 3\theta - 1}{\tan 3\theta + 1} = \sqrt{3}$ , then the general value of  $\theta$  is
- (a)  $\frac{n\pi}{3} + \frac{\pi}{12}$                       (b)  $\frac{n\pi}{3} + \frac{7\pi}{36}$   
 (c)  $n\pi + \frac{7\pi}{12}$                       (d)  $n\pi + \frac{\pi}{12}$
18. The equation  $\sin x + \cos x = 2$  has  
 (a) One solution  
 (b) Two solutions  
 (c) Infinite number of solutions  
 (d) No solutions
19. The number of values of  $\theta$  in  $[0, 2\pi]$  satisfying the equation  $2\sin^2 \theta = 4 + 3 \cos \theta$  are  
 (a) 0                      (b) 1                      (c) 2                      (d) 3
20. The most general value of  $\theta$  which will satisfy both the equations  $\sin \theta = -\frac{1}{2}$  and  $\tan \theta = \frac{1}{\sqrt{3}}$  is  
 (a)  $n\pi + (-1)^n \frac{\pi}{6}$                       (b)  $n\pi + \frac{\pi}{6}$   
 (c)  $2n\pi \pm \frac{\pi}{6}$                       (d) None of these

### SECTION - B

#### INTEGER TYPE QUESTIONS

21. If  $n$  arithmetic means are inserted between  $a$  and  $100$  such that the ratio of the first mean to the last mean is  $1 : 7$  and  $a + n = 33$ , then the value of  $n$  is \_\_\_\_\_.
22. If  $3^{2\sin 2\alpha - 1}, 14$  and  $3^{4 - 2\sin 2\alpha}$  are the first three terms of an A.P. for some  $\alpha$ , then the sixth term of this A.P. is \_\_\_\_\_.
23. Let  $a_1 = 8, a_2, a_3, \dots, a_n$  be an A.P. If the sum of its first four terms is  $50$  and the sum of its last four terms is  $170$ , then the product of its middle two terms is  $58K$  then the value of  $K$  is \_\_\_\_\_.
24. The number of terms common to the two A.P.'s  $3, 7, 11, \dots, 407$  and  $2, 9, 16, \dots, 709$  is \_\_\_\_\_.
25. The value of  $(0.16)^{\log_{25} \left( \frac{1}{3} + \frac{1}{3^2} + \frac{1}{3^3} + \dots \right)}$  is equal to \_\_\_\_\_.
26. If  $(20)^{19} + 2(21)(20)^{18} + 3(21)^2(20)^{17} + \dots + 20(21)^{19} = k(20)^{19}$ , then  $k$  is equal to  $25K$  then the value of  $K$  is \_\_\_\_\_.
27. If  $\frac{1}{2 \times 3 \times 4} + \frac{1}{3 \times 4 \times 5} + \frac{1}{4 \times 5 \times 6} + \dots + \frac{1}{100 \times 101 \times 102} = \frac{K}{101}$ , then  $9.4K$  is equal to \_\_\_\_\_.
28. The value of  $\tan 9^\circ - \tan 27^\circ - \tan 63^\circ + \tan 81^\circ$  is \_\_\_\_\_.
29. If  $\sin^2(10^\circ) \sin(20^\circ) \sin(40^\circ) \sin(50^\circ) \sin(70^\circ) = \alpha - \frac{1}{16} \sin(10^\circ)$  then  $16 + \alpha^{-1}$  is equal to \_\_\_\_\_.
30. The number of solutions of  $|\cos x| = \sin x$ , such that  $-4\pi \leq x \leq 4\pi$  is \_\_\_\_\_.